

# MATH 123 PRACTICE MIDTERM 3

NAME (PRINTED):

DISCUSSION TIME:

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Please *turn off all electronic devices*. You may use both sides of a  $8.5 \times 11$  sheet of paper for notes while you take this exam. No calculators, no course notes, no books, no help from your neighbors. **Show all work**—the grading will be based on your work shown as well as the end result. Remember to put your name at the top of this page. Good luck.

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Problem	Score (out of)
1	(10)
2	(10)
3	(10)
4	(10)
5	(10)
6	(10)
7	(10)
<b>Total</b>	(70)

1. (10 pts) Evaluate the following limit. Carefully justify your answer.

$$\lim_{n \rightarrow \infty} \frac{\sin(n) \ln(n)}{n}$$

2. (10 pts) Evaluate the following series

$$\sum_{n=0}^{\infty} \frac{3^{n-1} + 4^{n+1} + 1}{5^n}$$

**3.** (10 pts) Find all values of  $k$  for which the following series converges. Carefully justify your answer.

$$\sum_{n=1}^{\infty} \frac{n+1}{kn^3 + n^2 + n + 1}$$

4. (10 pts) Determine if the following series converges or diverges. Carefully justify your answer.

$$\sum_{n=1}^{\infty} \left(1 + \frac{1}{n}\right)^{\frac{1}{100}n^2}$$

5. Show that the following series converges conditionally. Carefully justify your answer.

$$\sum_{n=1}^{\infty} \frac{(-1)^n \ln(n)}{n}$$

6. (10 pts) Find the interval of convergence for the following power series.

$$\sum_{n=1}^{\infty} \frac{(n!)^2 x^n}{(2n)!}$$